



ΠΑΡΑΓΩΓΟΙ

$$(c)' = 0$$

$$\text{Θέτω ότι : } f(x) = z$$

$$(x^v)' = vx^{v-1}$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(e^x)' = e^x$$

$$(e^z)' = z'e^z$$

$$(\ln x)' = \frac{1}{x}$$

$$(\ln z)' = \frac{z'}{z}$$

$$(a^x)' = a^x \ln a$$

$$(a^z)' = z'a^z \ln a$$

$$(\eta \mu x)' = \sigma \upsilon \nu x$$

$$(\eta \mu z)' = z'\sigma \upsilon \nu z$$

$$(\sigma \upsilon \nu x)' = -\eta \mu x$$

$$(\sigma \upsilon \nu z)' = -z'\eta \mu z$$

$$(\epsilon \phi x)' = \tau \epsilon \mu^2 x$$

$$(\epsilon \phi z)' = z'\tau \epsilon \mu^2 z$$

$$(\sigma \phi x)' = -\sigma \tau \epsilon \mu^2 x$$

$$(\sigma \phi z)' = -z'\sigma \tau \epsilon \mu^2 z$$

$$(\tau \epsilon \mu x)' = \tau \epsilon \mu x \epsilon \phi x$$

$$(\tau \epsilon \mu z)' = z'\tau \epsilon \mu z \epsilon \phi z$$

$$(\sigma \tau \epsilon \mu z)' = \sigma \tau \epsilon \mu x \sigma \phi x$$

$$(\sigma \tau \epsilon \mu z)' = -z'\sigma \tau \epsilon \mu z \sigma \phi z$$

Κανόνες παραγωγικής

$$(u + v)' = u' + v'$$

$$(u \cdot v)' = u' \cdot v + u \cdot v'$$

$$\left(\frac{u}{v}\right)' = \frac{u' \cdot v - u \cdot v'}{v^2}$$

$$(c \cdot u)' = c \cdot u'$$

Παράγωγος συνάρτησης που ορίζεται παραμετρικά

$$\text{Αν } x = f(t)$$

$$\text{τότε } \frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}$$

$$y = g(t)$$

$$\text{και } \frac{d^2 y}{dx^2} = \frac{d}{dt} \left(\frac{dy}{dx} \right) \frac{dt}{dx}$$